

1. Use the differential area $d\mathbf{S}$ to calculate the area of the surface defined by $\rho = 5$, $\pi/2 < \phi < \pi$, and $-2 < z < 2$. [5]

2. Convert the vector $\mathbf{P} = y^2\mathbf{p}_x + (x + 1)\mathbf{p}_y + yz\mathbf{p}_z$ into cylindrical coordinates. [5]

3. Given two points, namely $A(2, 60^\circ, 2)$ and $B(2\sqrt{3}, 30^\circ, 3)$, find the corresponding position vectors \mathbf{A} and respectively \mathbf{B} . Then find the unit vector in the direction from \mathbf{A} to \mathbf{B} .

4. Find $\nabla^2 \mathbf{B}$ when $\mathbf{B} = r^2 \mathbf{b}_r + \sin \theta \mathbf{b}_\theta + \cos^2 \theta \mathbf{b}_\phi$.